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RANDOM NUMBER GENERATOR PACKAGE LLRANDOM

by

G. P. Learmonth

and

P. A. W. Lewis

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ABSTRACT

This report is intended to describe an interim version of a computer program package for random number generation on the IBM System/360. The package, when called by a FORTRAN IV program, will deliver either a single value or an array (of specified size) of single precision uniformly, normally, or exponentially distributed pseudo-random deviates, or a single value or an array of uniformly distributed integers between 1 and $2^{31}-1$. The package also has the ability (optional) to "shuffle" the pseudo-random numbers to obtain "better" statistical properties.

Prepared by:

NAVAL POSTGRADUATE SCHOOL

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I. Introduction.

Numerous random number generators have been proposed for the System/360. Several of these generators have been incorporated into the subroutine library here at the Computer Center. The adequacy of some of these generators has rested on the results of some rather weak tests for randomness; recent results in the literature have shown many of these generators to be very poor performers. This report will describe an interim version of a package for random number generation which has stood up under intensive statistical testing and is deemed to be very satisfactory for the System/360. (The statistical testing will be reported elsewhere.)

The package, when called by a FORTRAN IV program, will deliver either a single value or an array (of specified size) of single precision, uniformly, normally, or exponentially distributed pseudo-random deviates or a single value or an array of pseudo-random integers uniformly distributed between 1 and $2^{31}-1$. The package also has the ability (optional) to "shuffle" the pseudo-random numbers to obtain "better" statistical properties.

Further refinements will be made to this generator; however, it is now available for use in an interim version under the name LLRANDOM. Future versions will be announced through the W. R. Church Computer Center Newsletter. The changes envisioned will be internal and aimed at increasing speed and efficiency of coding. The actual numbers produced in future versions will remain the same as described here, as will the FORTRAN calling sequence.

Some definitions. By "random number generator" or "pseudo-random number generator" is meant an algorithm by which sequences of numbers

are produced which follow a given probability distribution and possess the appearance of randomness. Without attempting to address the still unresolved philosophical question of what a random sequence is, the underlined words above are the keys to random number generation on a digital computer. The term sequence implies that many random numbers must be produced serially from the algorithm. The user may need only a very few of these numbers, however we generally require that the algorithm be able to produce very many numbers. Distribution implies that we can associate a probability statement with the occurrence of each random number. The distribution is usually taken to be uniform, that is, within a given range the probability of occurrence of a given number is the same as for any other number in a similar range. If the algorithm produces, say, m distinct numbers then the probability of occurrence for any one of them is 1/m.

Lastly, we speak of the appearance of randomness. As will be shown next, the actual implementation of the algorithm is a recurrence relation where each succeeding number is a function of the preceding number. True randomness would require independence of successive numbers; however, the algorithm generates a deterministic sequence. Algorithms for random number generation do, however, yield sequences which appear to be random, hence the term "pseudo-random numbers." It is this characteristic which is the subject of statistical testing, that is, one asks, "how random does the given sequence appear?"

The uniform random number generator which forms the basis of the package described here is a Lehmer congruential generator. The recurrence relation is given by

$$X_n \equiv A \cdot X_{n-1} + C \pmod{m}. \qquad (1)$$

This generator produces integer random numbers between 1 and m. These integer values may then be transformed into real-valued numbers between 0.0 and 1.0 or into any desired distribution by an appropriate transformation.

II. The Generator.

The recurrence relation given in equation (1) is actually called a "Lehmer mixed congruential generator." The term mixed comes from the fact that it involves a multiplication by a constant, A, plus an addition of a constant, C. The actual implementation used in LLRANDOM is called a "multiplicative," or "pure," congruential generator in that we take $C = 0$, giving

$$X_n \equiv A \cdot X_{n-1} \pmod{m}. \qquad (2)$$

The field of positive integers is, of course, infinite. It is a reality of digital computers that only a finite number of positive integers are expressible. Specifically, we are limited to the word size of the System/360. This word size is 32 bits with one bit reserved for the algebraic sign; hence, an obvious choice for m is 2^{31}. The product $A \cdot X_{n-1}$ is formed by the System/360 in two adjacent registers yielding a result which may be as large as 2^{63}. We must, however, reduce this product to a number less than or equal to 2^{31}. The mod, or modulo, operation accomplishes this. The product $A \cdot X_{n-1}$ is divided by 2^{31} leaving a quotient which is some multiple of 2^{31} and a remainder which is strictly less than 2^{31}. It is this remainder which is the next pseudo-random number X_n in the equation (1).

On first examination it would appear that a full 2^{31} numbers could be generated by the sequence (1). This is not the case, unless A and m are chosen properly. We define a term called the period which is the number of unique random numbers computable for a given choice of A and m. To illustrate the concept, assume we have a six-bit word with one bit for a sign. We then have $m = 2^5 = 32$. Choose $A = 9$ and work through a sequence starting with $X_0 = 1$.

Step n	X_{n-1}	$A \cdot X_{n-1}$	$A \cdot X_{n-1} \pmod{2^5}$
1	1	9	9
2	9	81	17
3	17	153	25
4	25	225	1
5	1	9	9
.	.	.	.
.	.	.	.
.	.	.	.

Note that the modulus of this generator is 32, however we have realized a period of only 4, that is the sequence of 1, 9, 17, 25, 1, 9, . . . repeats after only 4 numbers. Obviously, care must be taken to insure that such occurrences do not happen in a random number generator. Hopefully, the period will also be independent of the starting value, X_0.

A great deal of work has been done on number theoretic considerations for the choice of m so as to yield a maximum period length (see Knuth[3]). To summarize, generators with modulus $m = 2^P$ for any integer, p, can have a maximum period of m/4, or, for the System/360, $2^{31}/4 = 2^{29}$; the period may also depend on the starting value. When the modulus m is a prime number, the maximum possible period is m - 1.

It so happens that the largest prime less than or equal to 2^{31} is $2^{31} - 1$, which is most fortuitous. Hence, choosing $m = 2^{31} - 1$ we can achieve a maximum period of $m - 1 = 2^{31} - 2$. These results produce only upper bounds on the period length. Recall in the example above, the maximum period possible is $2^5/4 = 2^3 = 8$, but that a period of only 4 was observed. This naturally leads to considerations of the choice of the multiplier, A.

Success in achieving a maximum period lies with the choice of the multiplier. Again, to briefly summarize the pertinent number theory, for a modulus 2^{31} the multiplier A must differ by 3 from the nearest multiple of 8; the starting value, X_0, must be odd; A must be one greater than a multiple of 4; and C must be odd. These conditions only assure a maximum period of m/4, not necessarily good statistical properties. For the random number generator described here (LLRANDOM) we are choosing C = 0; hence, this length is not achievable if $m = 2^{31}$. Luckily, the conditions on choosing A for the modulus $m = 2^{31} - 1$ are more easily met and we can achieve the maximum period.

Utilizing some of the nice number theoretic properties of the number $2^{31} - 1$, to achieve a maximum period, A must be a positive primitive root of $2^{31} - 1$ or a power of such a number. This is generally not easy to find; the value of A used in the generator described here is 7^5. The number 7 is a positive primitive root of $2^{31} - 1$ and raising 7 to the fifth power results in the multiplier 16807 which is also a positive primitive root of $2^{31} - 1$ (Lewis, Goodman, and Miller[1]) and satisfies some conditions regarding the statistical performance of the generated sequence. These conditions will not be discussed here.

The generator

$$X_n \equiv 7^5 \cdot X_{n-1} \pmod{2^{31}-1} \qquad (3)$$

is the generator reported in Lewis, Goodman, and Miller[1]. The authors cite the results of very extensive tests on this generator, all of which show that it is very satisfactory.

A. Division simulation. A practical consideration for random number generators is that they be fast, hopefully without requiring excessive memory to achieve speed. In many applications rather large quantities of numbers are needed and the speed of the generator can be crucial.

Nearly all random number generators are coded as subroutine or function subprograms in the assembler or machine language of the computer. The algorithm for implementing (3) is rather simple, involving a multiplication and then a division to effect the modulo operation. On most computers the division operation is rather slow as compared to the multiplication operation. In the past, the multiplier A was chosen so that its binary representation contained many zeroes, thereby speeding the multiplication. Unfortunately, this choice was at the expense of the period length, since such multipliers rarely met the number theoretic conditions for a maximum period. For the LLRANDOM generator (3) described here, the division operation has been replaced by a division simulation involving two shifts and an add instruction. Should a fixed-point (integer) overflow occur, two more additions are required to correct the situation.

The ordinary division on a System/360 Model 67-2 requires 8.49 micro-seconds. Without overflow, the simulation requires only 3.45

micro-seconds. When overflow occurs, the simulation takes an additional 2.32 micro-seconds for a total of 5.77 micro-seconds. These overflows occur quite rarely, on the order of only once in 250,000 iterations.

The division simulation algorithm (again due to Lehmer) is discussed by Payne, Rabung, and Bogyo[2] and works as follows. Define a congruence relationship by

$$X'_n \equiv A \cdot X_{n-1} \pmod{2^{31}}. \tag{4}$$

Performing the modulo operation on the product AX_{n-1} would give

$$AX_{n-1} = q2^{31} + r, \tag{5}$$

where q is some quotient and r is the remainder and is strictly less than 2^{31}. Adding q to both sides of (4) we get

$$X_n = X'_n + q \equiv AX_{n-1} \pmod{2^{31}-1}. \tag{6}$$

This form gives the desired modulus of $2^{31} - 1$, if there is no overflow in the addition of $X'_n + q$. If there is overflow, to correct it we merely add a constant of 1 to get

$$X_n \equiv X'_n + q + 1 \pmod{2^{31}} = A \cdot X_{n-1} \pmod{2^{31}-1}, \tag{7}$$

which is again, the desired result.

This division simulation algorithm is very easily implemented on the System/360 and saves considerable execution time over conventional division.

B. Shuffling. The sequence produced by the generator (3) does appear to consist of independent, uniformly distributed numbers for most purposes.

We realize that the numbers are not actually independent, due to the procedure used to generate them. It has been proposed that a sequence of such numbers be further randomized, or "shuffled," to improve upon the appearance of randomness (see, for instance, Knuth[3]). Serial correlation tests are usually employed to detect lack of independence in a sequence and at least one generator, RANDU, known to perform badly in a three-dimensional serial test was improved by shuffling. These tests will be discussed elsewhere. The various shuffling procedures which have been put forward have had little empirical validation.

The package described here has a built-in shuffling mechanism and it works as follows. A table of 128 random integers is maintained in the package. The starting values in the table represent members of the sequence (3) lagged by one million integers starting with an arbitrary seed. When a new integer is generated by the algorithm, its right-most seven bits are masked-off to form an index into the table (2^7=128). The integer in the table indexed by the right-most seven bits is returned to the caller and that table entry is replaced by the integer just generated. In essence, we are taking "chunks" of 128 numbers from the basic sequence and shuffling them before they are used.

This particular shuffling scheme is dependent on the choice of the modulus. For a modulus of 2^{31} the right-most bits of a congruential random number generator are non-random and their use in this scheme would defeat the purpose of shuffling. However, with a modulus of $2^{31} - 1$ and the positive primitive root multiplier $A = 7^5$, the right-most bits are quite random and the desired results are obtained.

C. Uniform (0.0,1.0) random numbers. So far, we have discussed how to generate uniform random integers over the range 1 to $m = 2^{31} - 1$. In most applications, uniform random numbers over the range 0.0 to 1.0 are desired. In theory, the uniform integers, X_i, are divided by m to produce these numbers, as

$$U_i = X_i/m. \tag{8}$$

In actual implementation on the System/360, the integer result is algebraically shifted right seven bits and a normalized floating point exponent is logically OR'ed on to it. The result is a properly normalized floating point random number over the range 0.0 to 1.0, usually referred to as a "real" uniform number.

D. Normally distributed random deviates. The uniformly distributed random numbers described above are not only useful in their own right, but form the basis of transformations into random numbers with other probability distributions. One of the most important of these distributions is the Normal distribution.

There are several methods of approximating a Normal distribution with uniform random numbers. One of the oldest and, unfortunately, most common is the "sum of k uniforms method." The algorithm is based on the fact that the uniform (0.0,1.0) distribution has a mean of 1/2 and a standard deviation of $\sqrt{1/12}$. The algorithm works as follows:

$$X = \frac{\sum_{i=1}^{k} U_i - k/2}{\sqrt{k/12.0}} \tag{9}$$

The random deviate X is approximately normally distributed with mean 0 and variance 1. The approximation is not as good as other methods and it is rather time consuming in that k uniforms must be generated and then summed. It was basically devised to overcome the very time consuming multiply and divide operations in older computers.

A more accurate algorithm is known as the Box-Muller method or Polar method which is actually a rejection method due to von Neumann. The method requires the generation of two uniforms to produce two independent Normals. It is based on the distribution of points inside the unit circle. The method is more accurate than the "sum of k uniforms method" (in fact, theoretically perfect). However, it does require two square roots and two natural logarithm operations which are generally rather time consuming.

The algorithm used in the package described here is based on a method developed by Marsaglia and is known as the "rectangle-wedge-tail" method. This algorithm is by far the fastest algorithm available for generating normally distributed random numbers, although it requires more memory than the Polar method.

The second volume of Knuth's "The Art of Computer Programming"[3] gives a complete and detailed description of the algorithm. Briefly, the positive half of the Normal density curve is discretized into 37 rectangles, wedges, and a tail as in Figure 1. All of the rectangles are uniformally distributed densities. The wedges are approximated by "nearly linear densities." Finally, the tail distribution is computed by a modification to the Polar method. The normal density, f(x), is then given by the composite function.

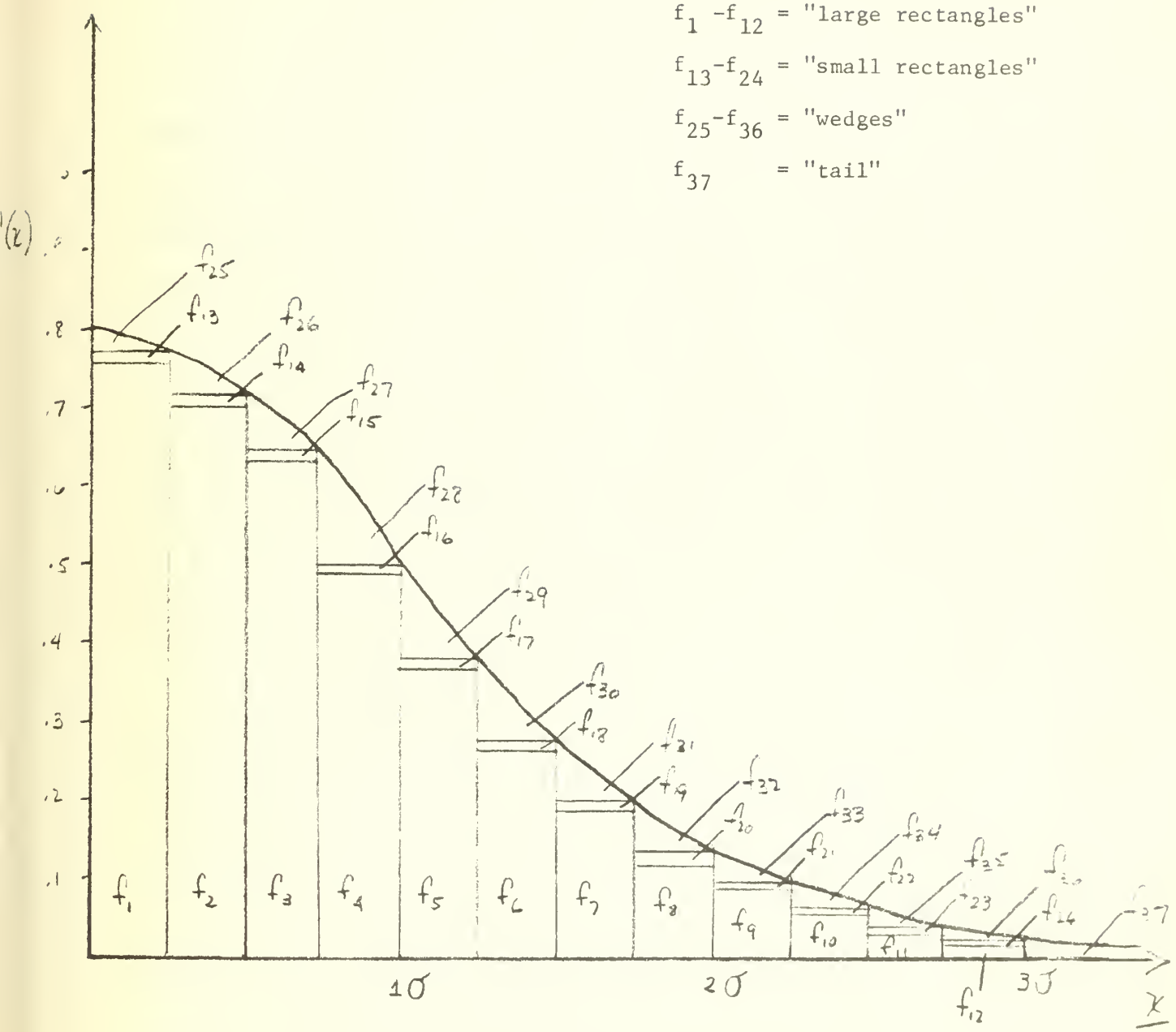

FIGURE 1

RECTANGLE-WEDGE-TAIL METHOD OF APPROXIMATING THE NORMAL DENSITY

$$f(x) = p_1 f_1(x) + p_2 f_2(x) + \ldots + p_{37} f_{37}(x), \qquad (10)$$

where

$$\sum_{i=1}^{37} p_i = 1,$$

the densities f_1 to f_{24} are the rectangles; f_{25} to f_{36} are the wedges; and f_{37} is the tail. The first twelve uniformly distributed rectangles are used 88% of the time. This makes for an extremely fast algorithm for the majority of deviates. When the tail is sampled, the deviate is generated by a modified Polar method and still quite satisfactory.

This generator for Normal deviates, like nearly all others, produces deviates with zero mean and unit variance. To change the scale and shape to any mean, μ, and the standard deviation, σ, we apply the linear transformation

$$Z = \mu + \sigma X \qquad (11)$$

where z now has the desired shape and scale parameters.

E. Exponential distribution. Another probability distribution of major interest in simulations is the exponential. The cumulative distribution function and probability density function for the exponential are respectively

$$F(x) = 1 - e^{-\lambda x}, \qquad (12)$$

$$f(x) = \lambda e^{-\lambda x}. \qquad (13)$$

The expected value of the exponential distribution is:

$$E[X] = 1/\lambda. \qquad (14)$$

The problem of generating exponential deviates reduces to one of generating "unit" exponentials, i.e. those with $\lambda = 1$, and then multiplying the result by whichever λ is necessary to give the desired distribution.

One of the most common methods of generating numbers from distributions other than the uniform is to use the inverse transformation technique (see Gaver and Thompson[4]). This can be described graphically, as in Figure 2, with a plot of the distribution function

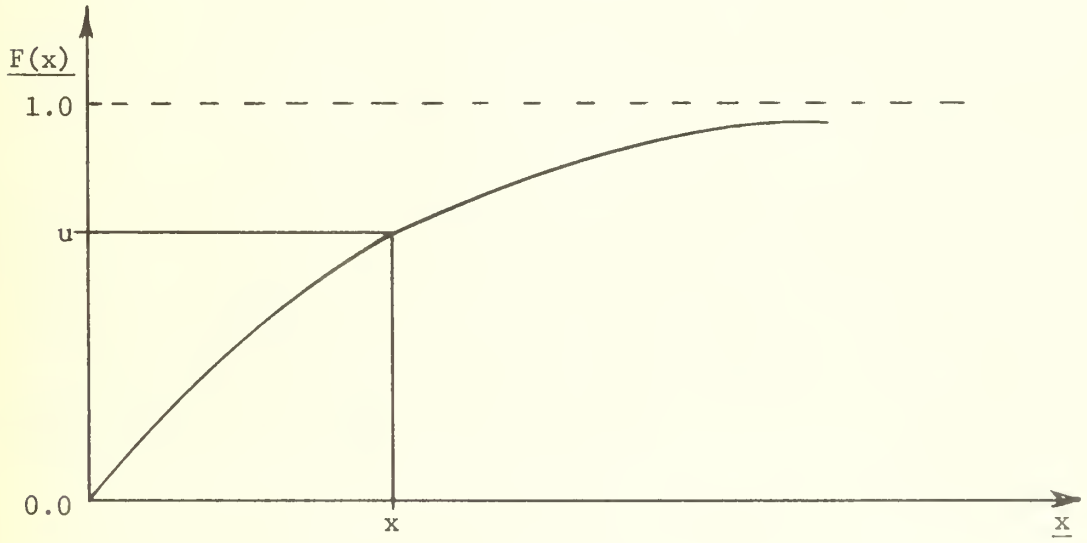

FIGURE 2.

CUMULATIVE DISTRIBUTION FUNCTION OF THE EXPONENTIAL DISTRIBUTION

The range of the abscissa, X, is infinite in extent. However, the range of the ordinate, F(x), is (0.0,1.0), the range of uniform (0,1) random variables. The inverse transformation technique is to generate a uniform random number, say U, and use this as the ordinate. The exponential deviate, say X, is the abscissa point corresponding to the intersection of the ordinate and the curve.

Mathematically, this technique is expressed as

$$u = F(x) = 1 - e^{-x}, \qquad \lambda = 1, \tag{15}$$

$$x = F^{-1}(u),$$

where u is the uniform random number. This inverse transformation is rather easily implemented for exponentially distributed random variables via natural logarithms since we get

$$F^{-1}(U) = -\ell n(1-U),$$

or by the symmetry of the uniform distribution

$$F^{-1}(U) = -\ell n(U).$$

Perhaps the most common implementation of exponential deviate generators is this natural logarithm transformation. It is mathematically appealing as well as trivial to program, given the usual FORTRAN subroutines.

The exponential deviate generator in the LLRANDOM package is based on Marsaglia's method of dividing the probability density into a series of rectangles, wedges, and a tail. Although more complicated to program and larger in size, this method is approximately 40% faster than the logarithmic transformation.

For a survey of the generation of normal and exponentially distributed variables see Ahrens and Dieter[5].

III. HOW TO USE THE PACKAGE.

The random number package described here is intended solely for use on the IBM System/360 or System/370 computers. The package consists of one Assembler F control section (CSECT) with nine entry points and two FORTRAN IV function subprograms. The names of the entry points and their functions are summarized in Table 1.

The subroutine entry point OVFLOW has no calling arguments and should be called once and only once at the beginning of the user's main FORTRAN program. The function subprograms RNORTH and REXPTH are called by the Assembler routine as needed and should not be called by the user. The eight additional entry points are the names of the actual routines to generate the random numbers. There are four types of random numbers which can be generated:

(1) uniformly distributed integers on the range 1 to $2^{31} - 1$;

(2) uniformly distributed single precision floating point numbers between 0.0 and 1.0;

(3) single precision floating point normal deviates with mean zero and variance 1; and

(4) single precision floating point exponential deviates with mean 1.

There is a separate entry point for each of the four types if shuffling of the sequence is desired.

For all eight entry points, the FORTRAN calling sequence is the same, namely:

CALL (entry point) (IX, A, N)

where

(entry point) refers to the routine desired,

viz. INT,SINT,RANDOM,SRAND,NORMAL,SNORM,EXPON, or SEXPON;

ENTRY POINT	FUNCTION
OVFLOW	Calls SPIE, handles fixed point overflows. (Must be called once at start of program.)
INT	Generates integer random numbers.
SINT	Generates shuffled integer random numbers.
RANDOM	Generates single precision floating point (0.0,1.0) random numbers.
SRAND	Generates single precision floating point (0.0,1.0) shuffled random numbers.
NORMAL	Generates single precision floating point normal deviates (μ=0,σ=1).
SNORM	Generates shuffled single precision floating point normal deviates (μ=0,σ=1).
EXPON	Generates single precision floating point exponential deviates (λ=1).
SEXPON	Generates shuffled single precision floating point exponential deviates (λ=1).

TABLE 1.

ENTRY POINT NAMES OF CONTROL SECTION OVFLOW

IX is the starting value of the sequence and may contain any integer number between 1 and 2147483647. This variable should not be altered by the user during the execution of the program, unless it is desired to repeat a sequence of random numbers.

A is either a scalar or vector variable and is the location with a specified dimension into which the random number or numbers are stored (see next parameter). Note that for entry points INT and SINT, this argument should be of INTEGER type.

N is an integer variable or constant designating how many random numbers are to be generated during this call. If N is greater than 1, A above must be a vector dimensioned at least as large as N. If N is equal to 1, then A may be scalar.

Some sample programs are given below:

(1) To generate 1000 consecutive integer random numbers:

```
INTEGER*4   M(1000)

CALL OVFLOW

IX = 1234567

--

--

--

CALL INT (IX, M, 1000)

--

END
```

(2) To generate 25 shuffled single precision floating point normal deviates and scale to mean 10 and standard deviation 5:

```
REAL*4   A(25)

CALL OVFLOW

JJ = 1936748

N = 25

--

--

--
```

```
      CALL SNORM (JJ, A, N)
      DO 1 I = 1,25
      A(I) = A(I)*5.0 + 10.0
    1 CONTINUE
      --
      --
      --
      END
```

(3) To generate one single precision floating point exponential deviate with mean 6:

```
      CALL OVFLOW
      I9 = 98367221
      --
      --
      --
      CALL EXPON (I9, E, 1)
      E = E*6.0
      --
      --
      --
      END
```

A. Implementation. LLRANDOM was designed and coded to run under Operating System/360 (OS). The Assembler Language control section contains a SPIE (Set Program Interrupt Exit) macro instruction which is a part of the OS Supervisor Services. This macro enables LLRANDOM to correct for the fixed point overflows resulting from the division simulation algorithm.

The remainder of the assembly coding is in Basic Assembler Language (BAL), i.e. no other macro calls or supervisor calls. To run LLRANDOM under another operating system for the System/360, an appropriate substitution for the SPIE macro would be necessary.

As currently programmed, LLRANDOM has the following memory requirements:

MODULE	SIZE IN BYTES (DECIMAL)
Assembler CSECT	3571
FORTRAN function RNORTH	1512
FORTRAN function REXPTH	1106
Total memory requirement	6189

The System/360 internal timer is rather crude for timing the execution of programs. The following times are therefore approximate timings for the generation of pseudo-random numbers on a System/360 Model 67-2.

ENTRY POINT	TIME IN MICROSECONDS	
INT	10.7	
SINT	15.7	
RANDOM	15.6	
SRAND	20.0	
NORMAL	57.5	(Polar method takes 349 microseconds)
SNORM	65.8	
EXPON	59.1	(Logarithm method takes 132 microseconds)
SEXPON	68.4	

B. Future Enhancements. The normal and exponential deviate routines in LLRANDOM are patterned after a package, SUPER-DUPER, available from Professor G. Marsaglia at McGill University in Montreal. It is available at the Naval Postgraduate School. Marsaglia uses a different multiplier, A, and modulus, m, in his congruential generator from that used in LLRANDOM and he then exclusive OR's this result with the output of a feedback shift register generator. SUPER-DUPER provides only one deviate per call and does not provide for shuffling the sequence.

The two FORTRAN function subprograms, RNORTH and REXPTH, are taken (with slight modification) directly from SUPER-DUPER. Among the changes to be made to LLRANDOM will be to rewrite RNORTH and REXPTH in System/360 Assembly Language and incorporate them directly into the package.

We have experienced occasions where large-scale simulations have been coded in FORTRAN using double precision variables. The fact that LLRANDOM returns single precision numbers causes some inconvenience. To alleviate this problem we will provide the capability in LLRANDOM to return single precision numbers into double precision variables or arrays. Note that the values returned will still be single precision; however, they will be stored properly into double precision locations.

Finally, additional entry points will be added to provide single precision floating point gamma deviates. Shuffling of the gamma deviates will also be available.

Other enhancements are under consideration.

```
***** NAVAL POSTGRADUATE SCHOOL RANDOM NUMBER GENERATOR : LLRANDOM *****

C RNOR TOOTH FUNCTION                                                    RNOR0010
      FUNCTION RNORTH(K,IX)                                              RNOR0020
      DIMENSION C(45)                                                    RNOR0030
      DATA C/Z40FD2B5F,Z40FD2B5F,Z40FAA9AD,Z40F5A648,Z40F32496,          RNOR0040
     $ Z40EE2131,Z40E69C1A,Z40E198B5,Z40DA139E,Z40D28E87,Z40C887BE,      RNOR0050
     $ Z40C102A6,Z40B6FBDD,Z40ACF513,Z40A2EE4A,Z4098E78C,Z40916269,      RNOR0060
     $ Z40875BAC,Z407D54D6,Z40734E0D,Z406BC8F6,Z4061C22C,Z405A3D15,      RNOR0070
     $ Z4052B7FE,Z404B32E7,Z4043ADD0,Z403C28B9,Z40372554,Z402FA03D,      RNOR0080
     $ Z402A9CD8,Z40259973,Z4020960E,Z401E145C,Z401910F7,Z40168F45,      RNOR0090
     $ Z40140D93,Z40118BE0,Z3FF0A2E4,Z3FC887BE,Z3FA06C98,Z3F785172,      RNOR0100
     $ Z3F785172,Z3F50364C,Z3F50364C,Z3F50364C/                          RNOR0110
      DATA I1/ZFBC35400/,I2/ZFE79702E/                                   RNOR0120
      IF(K.GT.I1)GO TO 3                                                 RNOR0130
      CALL RANDOM(IX,S,1)                                                RNOR0140
      CALL RANDOM(IX,T,1)                                                RNOR0150
      B=AINT(7.*(S+T)+37.*ABS(S-T))                                      RNOR0160
      CALL RANDOM(IX,Z9,1)                                               RNOR0170
      CALL RANDOM(IX,Z8,1)                                               RNOR0180
        X=Z9-Z8                                                          RNOR0190
      RNORTH=.0625*(X+SIGN(B,X))                                         RNOR0200
      RETURN                                                             RNOR0210
3     IF(K.GT.I2)GO TO 5                                                 RNOR0220
4     CALL RANDOM(IX,Z9,1)                                               RNOR0230
      CALL RANDOM(IX,Z8,1)                                               RNOR0240
      IF(Z8.GT.0.50) Z9=-Z9                                              RNOR0250
      RNORTH=2.75*Z9                                                     RNOR0260
      J=16.*ABS(RNORTH)+1.                                               RNOR0270
      IF(J-14) 6,6,7                                                     RNOR0280
   6  P=(J+J-1)*.1497466E-2                                              RNOR0290
      GO TO 8                                                            RNOR0300
   7  P=(89-J-J)*.698817E-3                                              RNOR0310
8     CALL RANDOM(IX,Z9,1)                                               RNOR0320
      IF(Z9.GT.79.78846*(EXP(-.5*RNORTH*RNORTH)                          RNOR0330
     $    -C(J)-P*(J-16.*ABS(RNORTH)))) GOTO4                            RNOR0340
      RETURN                                                             RNOR0350
5     CALL RANDOM(IX,V,1)                                                RNOR0360
      CALL RANDOM(IX,Z9,1)                                               RNOR0370
      IF(Z9.GT.0.5) V=-V                                                 RNOR0380
      IF(V.EQ.0) GO TO 5                                                 RNOR0390
      X=SQRT(7.5625-2.*ALOG(ABS(V)))                                     RNOR0400
      CALL RANDOM (IX,Z9,1)                                              RNOR0410
      IF(Z9*X.GT.2.75) GO TO 5                                           RNOR0420
      RNORTH=SIGN(X,V)                                                   RNOR0430
      RETURN                                                             RNOR0440
      END                                                                RNOR0450
```

```
OVFLOW   CSECT                                                          LLRA0010
         EXTRN RNORTH,REXPTH                                            LLRA0020
         ENTRY INT,SINT,RANDOM,SRAND,NORMAL,SNORM,EXPON,SEXPON          LLRA0030
         USING OVFLOW,R12                                               LLRA0040
         B     12(,R15)          BRANCH AROUND ID                       LLRA0050
         DC    AL1(6)                                                   LLRA0060
         DC    CL6'OVFLOW'                                              LLRA0070
         STM   R14,R12,12(R13)   SAVE REGISTERS IN HIGH SAVE AREA       LLRA0080
         LR    R12,R15           ESTABLISH BASE ADDRESS                 LLRA0090
         ST    R13,SA+4          SAVE CALLER'S R13                      LLRA0100
         LR    R2,R13                                                   LLRA0110
         LA    R13,SA            NEW SAVE AREA                          LLRA0120
         ST    R13,8(,R2)        STORE WITH CALLING ROUTINE             LLRA0130
*                                                                       LLRA0140
****  ISSUE SPIE TO GET FIXED POINT OVERFLOWS AS WELL AS FORTRAN        LLRA0150
****  INTERRUPTS.                                                       LLRA0160
*                                                                       LLRA0170
         SPIE  FIXIT,(8,9,12,13,15)                                     LLRA0180
         ST    R1,PICA           SAVE FORTRAN'S PICA ADDRESS            LLRA0190
         L     R13,SA+4          RESTORE CALLER'S R13                   LLRA0200
         LM    R14,R12,12(R13)   RESTORE THE REGISTERS                  LLRA0210
         BCR   15,R14            RETURN                                 LLRA0220
```

```
*                                                                      LLRA0240
*     SPIE BRINGS US HERE ON INTERRUPTS                                LLRA0250
*                                                                      LLRA0260
          USING *,R15                                                  LLRA0270
FIXIT     TM    7(R1),X'F7'     WAS IT A FIXED POINT OVERFLOW?         LLRA0280
          BC    5,FORT          NO, LET FORTRAN'S SPIE HANDLE IT       LLRA0290
          CLC   17(3,R1),AINT+1   TEST WHETHER BASE OF INTERRUPTED     LLRA0300
          BL    0(,R14)             ROUTINE WAS BETWEEN ENTRIES INT AND LLRA0310
          CLC   17(3,R1),ASEXPO+1     SEXPON INCLUSIVE; IF NOT, IGNORE LLRA0320
          BH    0(,R14)                 THE INTERRUPT                  LLRA0330
          A     R4,PM2          ADD 2**31-3                            LLRA0340
          AR    R4,R2           ADD 4 MORE TO MAKE 2**31+1 CORRECTION  LLRA0350
          BR    R14             ALL FIXED, CONTINUE                    LLRA0360
FORT      L     R15,PICA        NOT FIXED POINT OVERFLOW, LET FORTRAN  LLRA0370
          L     R15,0(,R15)       EXTENDED ERROR HANDLING RCUTINE      LLRA0380
          BR    R15                 TAKE CARE OF IT                    LLRA0390
```

```
*                                                                      LLRA0410
*    ENTRY POINT :  INT                                                LLRA0420
*                                                                      LLRA0430
         CNOP  0,8                                                     LLRA0440
         USING INT,R15          BASE REGISTER                          LLRA0450
INT      B     8(,R15)          BRANCH AROUND ID                       LLRA0460
         DC    AL1(3)                                                  LLRA0470
         DC    CL3'INT'                                                LLRA0480
         STM   R14,R12,12(R13) SAVE REGISTERS IN HIGH SAVE AREA        LLRA0490
         ST    R13,SA+4         ADDRESS OF HIGH SAVE AREA IN LOW SAVE AR. LLRA0500
         LR    R2,R13           COPY TO R2                             LLRA0510
         LA    R13,SA           ADDRESS OF LOW SAVE AREA               LLRA0520
         ST    R13,8(,R2)       ADDRESS OF LOW SAVE AREA IN HIGH SAVE AR. LLRA0530
         L     R9,A75           LOAD MULTIPLIER                        LLRA0540
         LA    R2,4             CONSTANT FOR BXLE                      LLRA0550
         LM    R5,R7,0(R1)      ADDRESSES OF THREE ARGUMENTS           LLRA0560
         L     R5,0(,R5)        LOAD STARTING VALUE INTO R5            LLRA0570
         L     R3,0(,R7)        NUMBER OF CONSECUTIVE WORDS TO FILL    LLRA0580
         SLA   R3,2             CONVERT TO BYTES                       LLRA0590
         SR    R6,R2            BACKUP ONE WORD IN CALLER'S ARRAY      LLRA0600
         LR    R7,R2            INITIAL VALUE FOR INDEX REGISTER       LLRA0610
         CNOP  0,8              ALIGN BXLE LOOP FOR SPEED              LLRA0620
L1       MR    R4,R9            FORM PRODUCT OF A AND X(N-1)           LLRA0630
         SLDA  R4,1             R4= REMAINDER ; R5 = QUOTIENT          LLRA0640
         SRL   R5,1               ADD QUOTIENT TO REMAINDER THEREBY    LLRA0650
         AR    R4,R5                SIMULATING DIVISION BY 2**31-1    LLRA0660
         LR    R5,R4            PUT X(N) INTO R5 FOR NEXT GC AROUND    LLRA0670
         ST    R5,0(R7,R6)      STORE IN CALLER'S ARRAY                LLRA0680
N1       BXLE  R7,R2,L1         LOOP AROUND AGAIN                      LLRA0690
         L     R4,0(,R1)        GET STARTING VALUE ADDRESS AGAIN       LLRA0700
         ST    R5,0(,R4)        STORE AS STARTING VALUE FOR NEXT CALL  LLRA0710
         L     R13,SA+4         RESTORE CALLER'S SAVE AREA POINTER     LLRA0720
         LM    R14,R12,12(R13) RESTORE THE REGISTERS                  LLRA0730
         BCR   15,R14           RETURN                                 LLRA0740
```

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***** NAVAL POSTGRADUATE SCHOOL RANDOM NUMBER GENERATOR : LLRANDOM *****

*                                                                      LLRA0760
*    ENTRY POINT : SINT                                                LLRA0770
*                                                                      LLRA0780
         CNOP  0,8                                                     LLRA0790
         USING SINT,R15        BASE REGISTER                           LLRA0800
SINT     B     10(0,R15)       BRANCH AROUND ID                        LLRA0810
         DC    AL1(4)                                                  LLRA0820
         DC    CL4'SINT'                                               LLRA0830
         STM   R14,R12,12(R13) SAVE REGISTERS IN HIGH SAVE AREA        LLRA0840
         ST    R13,SA+4        ADDRESS OF HIGH SAVE AREA IN LOW SAVE AR. LLRA0850
         LR    R2,R13          COPY TO R2                              LLRA0860
         LA    R13,SA          ADDRESS OF LOW SAVE AREA                LLRA0870
         ST    R13,8(,R2)      ADDRESS OF LOW SAVE AREA IN HIGH SAVE AR. LLRA0880
         L     R9,A75          LOAD MULTIPLIER                         LLRA0890
         LA    R2,4            CONSTANT FOR BXLE                       LLRA0900
         LM    R5,R7,0(R1)     ADDRESSES OF THREE ARGUMENTS            LLRA0910
         L     R5,0(,R5)       LOAD STARTING VALUE INTO R5             LLRA0920
         L     R3,0(,R7)       NUMBER OF CONSECUTIVE WORDS TO FILL     LLRA0930
         SLA   R3,2            CONVERT TO BYTES                        LLRA0940
         SR    R6,R2           BACKUP ONE WORD IN CALLER'S ARRAY       LLRA0950
         LR    R7,R2           INITIAL VALUE FOR INDEX REGISTER        LLRA0960
         LA    R8,TABLE        ADDRESS OF SHUFFLING TABLE              LLRA0970
         L     R1,MASK         INDEX MASK FOR SHUFFLING                LLRA0980
         CNOP  0,8             ALIGN BXLE LOOP FOR SPEED               LLRA0990
L2       MR    R4,R9           FORM PRODUCT OF A AND X(N-1)            LLRA1000
         SLDA  R4,1            R4 = REMAINDER ; R5 = QUOTIENT          LLRA1010
         SRL   R5,1              ADD QUOTIENT TO REMAINDER THEREBY     LLRA1020
         AR    R4,R5               SIMULATING DIVISION BY 2**31-1      LLRA1030
         LR    R5,R4           PUT X(N) INTO R5 FOR NEXT GC AROUND     LLRA1040
         NR    R4,R1           EXTRACT RIGHT-MOST 7 BITS               LLRA1050
         SLA   R4,2            CONVERT TO BYTE OFFSET IN TABLE         LLRA1060
         L     R0,0(R4,R8)     SELECT RANDOM TABLE VALUE               LLRA1070
         ST    R5,0(R4,R8)     REPLACE TABLE VALUE WITH X(N)           LLRA1080
         ST    R0,0(R7,R6)     RANDOM TABLE VALUE TO CALLER'S ARRAY    LLRA1090
N2       BXLE  R7,R2,L2        LOOP AROUND AGAIN                       LLRA1100
         L     R13,SA+4        RESTORE CALLER'S SAVE AREA POINTER      LLRA1110
         L     R1,24(,R13)     GET ARGUMENT LIST POINTER AGAIN         LLRA1120
         L     R4,0(,R1)       GET STARTING VALUE ADDRESS AGAIN        LLRA1130
         ST    R5,0(,R4)       STORE AS STARTING VALUE FOR NEXT CALL   LLRA1140
         LM    R14,R12,12(R13) RESTORE THE REGISTERS                   LLRA1150
         BCR   15,R14          RETURN                                  LLRA1160
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***** NAVAL POSTGRADUATE SCHOOL RANDOM NUMBER GENERATOR : LLRANDOM *****

*                                                                      LLRA1180
*     ENTRY PCINT :  RANDOM                                            LLRA1190
*                                                                      LLRA1200
          CNOP  0,8                                                    LLRA1210
          USING RANDOM,R15      BASE REGISTER                          LLRA1220
RANDOM    B     12(,R15)        BRANCH AROUND ID                       LLRA1230
          DC    AL1(6)                                                 LLRA1240
          DC    CL6'RANDOM'                                            LLRA1250
          STM   R14,R12,12(R13) SAVE REGISTERS IN HIGH SAVE AREA       LLRA1260
          ST    R13,SA+4        ADDRESS OF HIGH SAVE AREA IN LOW SAVE AR. LLRA1270
          LR    R2,R13          COPY TO R2                             LLRA1280
          LA    R13,SA          ADDRESS OF LOW SAVE AREA               LLRA1290
          ST    R13,8(,R2)      ADDRESS OF LOW SAVE AREA IN HIGH SAVE AR. LLRA1300
          LM    R9,R11,A75      LOAD MULTIPLIER AND NORMALIZATION CONST. LLRA1310
          LA    R2,4            CONSTANT FOR BXLE                      LLRA1320
          LM    R5,R7,0(R1)     ADDRESSES OF THREE ARGUMENTS           LLRA1330
          L     R5,0(,R5)       LOAD STARTING VALUE INTO R5            LLRA1340
          L     R3,0(,R7)       NUMBER OF CONSECUTIVE WORDS TO FILL    LLRA1350
          SLA   R3,2            CONVERT TO BYTES                       LLRA1360
          SR    R6,R2           BACKUP ONE WORD IN CALLER'S ARRAY      LLRA1370
          LR    R7,R2           INITIAL VALUE FOR INDEX REGISTER       LLRA1380
          SUR   FR0,FR0         CLEAR FLOATING POINT REGISTER 0        LLRA1390
          LA    R12,N3          ADDRESS OF BXLE INSTRUCTICN            LLRA1400
          LA    R13,M3          ADDRESS OF NORMALIZATION ROUTINE       LLRA1410
          CNOP  0,8             ALIGN BXLE LOOP FOR SPEED              LLRA1420
L3        MR    R4,R9           FORM PRODUCT OF A AND X(N-1)           LLRA1430
          SLDA  R4,1            R4 = REMAINDER ; R5 = QUOTIENT         LLRA1440
          SRL   R5,1              ADD QUOTIENT TC REMAINDER THEREBY    LLRA1450
          AR    R4,R5               SIMULATING DIVISION BY 2**31-1     LLRA1460
          LR    R5,R4           PUT X(N) INTO R5 FOR NEXT GO AROUND    LLRA1470
          SRL   R4,7            MAKE ROOM FOR THE EXPONENT             LLRA1480
          OR    R4,R10          OR ON THE EXPONENT                     LLRA1490
          ST    R4,0(R7,R6)     STORE IN CALLER'S ARRAY                LLRA1500
          CR    R4,R11          DID IT NEED NORMALIZATION?             LLRA1510
          BCR   4,R13           YES, GO NORMALIZE IT                   LLRA1520
N3        BXLE  R7,R2,L3        LOOP AROUND AGAIN                      LLRA1530
          L     R4,0(,R1)       GET STARTING VALUE ADDRESS AGAIN       LLRA1540
          ST    R5,0(,R4)       STORE AS STARTING VALUE FOR NEXT CALL  LLRA1550
          L     R13,SA+4        RESTORE CALLER'S SAVE AREA POINTER     LLRA1560
          LM    R14,R12,12(R13) RESTORE THE REGISTERS                  LLRA1570
          BCR   15,R14          RETURN                                 LLRA1580
M3        LE    FR2,0(R7,R6)    LOAD INTO FLOATING POINT REGISTER 2    LLRA1590
          AER   FR2,FR0         ADD ZERO AND NORMALIZE                 LLRA1600
          STE   FR2,0(R7,R6)    STORE BACK NORMALIZED                  LLRA1610
          BR    R12             CONTINUE THE BXLE LOOP                 LLRA1620
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*                                                                      LLRA1640
*     ENTRY POINT :  SRAND                                             LLRA1650
*                                                                      LLRA1660
          CNOP  0,8                                                    LLRA1670
          USING SRAND,R15       BASE REGISTER                          LLRA1680
SRAND     B     10(,R15)        BRANCH AROUND ID                       LLRA1690
          DC    AL1(5)                                                 LLRA1700
          DC    CL5'SRAND'                                             LLRA1710
          STM   R14,R12,12(R13) SAVE REGISTERS IN HIGH SAVE AREA       LLRA1720
          ST    R13,SA+4        ADDRESS OF HIGH SAVE AREA IN LOW SAVE AR. LLRA1730
          LR    R2,R13          COPY TO R2                             LLRA1740
          LA    R13,SA          ADDRESS OF LOW SAVE AREA               LLRA1750
          ST    R13,8(,R2)      ADDRESS OF LOW SAVE AREA IN HIGH SAVE AR. LLRA1760
          LM    R9,R11,A75      LOAD MULTIPLIER AND NORMALIZATION CONST. LLRA1770
          LA    R2,4            CONSTANT FOR BXLE                      LLRA1780
          LM    R5,R7,0(R1)     ADDRESSES OF THREE ARGUMENTS           LLRA1790
          L     R5,0(,R5)       LOAD STARTING VALUE INTO R5            LLRA1800
          L     R3,0(,R7)       NUMBER OF CONSECUTIVE WORDS TO FILL    LLRA1810
          SLA   R3,2            CONVERT TO BYTES                       LLRA1820
          SR    R6,R2           BACKUP ONE WORD IN CALLER'S ARRAY      LLRA1830
          LR    R7,R2           INITIAL VALUE FOR INDEX REGISTER       LLRA1840
          SUR   FR0,FR0         CLEAR FLOATING POINT REGISTER 0        LLRA1850
          LA    R12,N4          ADDRESS OF BXLE INSTRUCTION            LLRA1860
          LA    R13,M4          ADDRESS OF NORMALIZATION ROUTINE       LLRA1870
          LA    R8,TABLE        ADDRESS OF SHUFFLING TABLE             LLRA1880
          L     R1,MASK         INDEX MASK FOR SHUFFLING               LLRA1890
          CNOP  0,8             ALIGN BXLE LOOP FOR SPEED              LLRA1900
L4        MR    R4,R9           FORM PRODUCT OF A AND X(N-1)           LLRA1910
          SLDA  R4,1            R4 = REMAINDER ; R5 = QUOTIENT         LLRA1920
          SRL   R5,1              ADD QUOTIENT TO REMAINDER THEREBY    LLRA1930
          AR    R4,R5               SIMULATING DIVISION BY 2**31-1     LLRA1940
          LR    R5,R4           PUT X(N) INTO R5 FOR NEXT GO AROUND    LLRA1950
          NR    R4,R1           EXTRACT RIGHT-MOST 7 BITS              LLRA1960
          SLA   R4,2            CONVERT TO BYTE OFFSET IN TABLE        LLRA1970
          L     R0,0(R4,R8)     SELECT RANDOM TABLE VALUE              LLRA1980
          ST    R5,0(R4,R8)     REPLACE TABLE VALUE WITH X(N)          LLRA1990
          SRL   R0,7            MAKE ROOM FOR THE EXPONENT             LLRA2000
          OR    R0,R10          OR ON THE EXPONENT                     LLRA2010
          ST    R0,0(R7,R6)     STORE IN CALLER'S ARRAY                LLRA2020
          CR    R0,R11          DID IT NEED NORMALIZATION ?            LLRA2030
          BCR   4,R13           YES, GO NORMALIZE IT                   LLRA2040
N4        BXLE  R7,R2,L4        LOOP AROUND AGAIN                      LLRA2050
          L     R13,SA+4        RESTORE CALLER'S SAVE AREA POINTER     LLRA2060
          L     R1,24(,R13)     GET ARGUMENT LIST POINTER AGAIN        LLRA2070
          L     R4,0(,R1)       GET STARTING VALUE ADDRESS AGAIN       LLRA2080
          ST    R5,0(,R4)       STORE AS STARTING VALUE FOR NEXT CALL  LLRA2090
          LM    R14,R12,12(R13) RESTORE THE REGISTERS                  LLRA2100
          BCR   15,R14          RETURN                                 LLRA2110
M4        LE    FR2,0(R7,R6)    LOAD INTO FLOATING POINT REGISTER 2    LLRA2120
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         AER    FR2,FR0          ADD ZERO AND NORMALIZE                    LLRA2130
         STE    FR2,0(R7,R6)     STORE BACK NORMALIZED                     LLRA2140
         BR     R12              CONTINUE THE BXLE LOOP                    LLRA2150
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*                                                                      LLRA2170
*     ENTRY POINT :  NORMAL                                            LLRA2180
*                                                                      LLRA2190
          CNOP  0,8                                                    LLRA2200
          USING NORMAL,R15      BASE REGISTER                          LLRA2210
NORMAL    B     12(,R15)        BRANCH AROUND ID                       LLRA2220
          DC    AL1(6)                                                 LLRA2230
          DC    CL6'NORMAL'                                            LLRA2240
          STM   R14,R12,12(R13) SAVE REGISTERS IN HIGH SAVE AREA       LLRA2250
          ST    R13,SA2+4       ADDRESS OF HIGH SAVE AREA IN LOW SAVE AR. LLRA2260
          LR    R2,R13          COPY TO R2                             LLRA2270
          LA    R13,SA2         ADDRESS OF LOW SAVE AREA               LLRA2280
          ST    R13,8(,R2)      ADDRESS OF LOW SAVE AREA IN HIGH SAVE AR. LLRA2290
          LM    R9,R11,A75N     LOAD MULTIPLIER,EXPONENT,AND TEST MASK LLRA2300
          LA    R2,4            CONSTANT FOR BXLE                      LLRA2310
          LM    R5,R7,0(R1)     ADDRESSES OF THREE ARGUMENTS           LLRA2320
          L     R5,0(,R5)       LOAD STARTING VALUE INTO R5            LLRA2330
          L     R3,0(,R7)       NUMBER OF CONSECUTIVE WORDS TO FILL    LLRA2340
          SLA   R3,2            CONVERT TO BYTES                       LLRA2350
          SR    R6,R2           BACKUP ONE WORD IN CALLER'S ARRAY      LLRA2360
          LR    R7,R2           INITIAL VALUE FOR INDEX REGISTER       LLRA2370
          LA    R13,ATBLE       ADDRESS OF TABLE OF CONSTANTS          LLRA2380
          LA    R12,N5          ADDRESS OF BXLE                        LLRA2390
          CNOP  0,8             ALIGN BXLE LOOP FOR SPEED              LLRA2400
L5        MR    R4,R9           FORM PRODUCT OF A AND X(N-1)           LLRA2410
          SLDA  R4,1            R4 = REMAINDER ; R5 = QUOTIENT         LLRA2420
          SRL   R5,1              ADD QUOTIENT TO REMAINDER THEREBY    LLRA2430
          AR    R4,R5               SIMULATING DIVISION BY 2**31-1     LLRA2440
          LR    R5,R4           PUT X(N) INTO R5                       LLRA2450
          LR    R0,R5           COPY R5 INTO R0 FOR NOW                LLRA2460
          NR    R4,R11          SHOULD WE MAKE IT NEGATIVE ?           LLRA2470
          BC    8,F1            POSITIVE, KEEP GOING                   LLRA2480
          LNR   R5,R5           MAKE R5 TRUE NEGATIVE                  LLRA2490
          SLR   R4,R4           CLEAR R4 TO ZERO                       LLRA2500
F1        CL    R5,C1           R5 LESS THAN X'68000000' ?             LLRA2510
          BC    11,F2           NO                                     LLRA2520
          SLDL  R4,8            SHIFT FIRST 8 BITS OF R5 INTO R4 AS INDEX LLRA2530
          IC    R4,0(R4,R13)    OBTAIN CONSTANT FROM TABLE             LLRA2540
          STC   R4,PWRD+1       STORE IN SECOND BYTE OF PWRD           LLRA2550
          SRL   R5,8            SHIFT REMAINING 24 BITS RIGHT THEN OR ON  LLRA2560
          ALR   R5,R10          EXPONENT TO MAKE  .(24 BITS)/16        LLRA2570
          ST    R5,0(R7,R6)     STORE IN CALLER'S ARRAY                LLRA2580
          LE    FR0,PWRD        LOAD CHARACTERISTIC TO FLOATING POINT  LLRA2590
          AE    FR0,0(R7,R6)    REGISTER 0 AND ADD FRACTION            LLRA2600
          STE   FR0,0(R7,R6)    STORE NORMAL DEVIATE IN CALLER'S ARRAY LLRA2610
          LR    R5,R0           COPY BACK TO R5 FOR NEXT GO AROUND     LLRA2620
          BR    R12             GO TO BXLE AND CONTINUE                LLRA2630
F2        CL    R5,C2           R5 LESS THAN X'D0000000' ?             LLRA2640
          BC    11,F3           NO                                     LLRA2650
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         SLDL  R4,8            SHIFT FIRST 8 BITS OF R5 INTO R4 AS INDEX LLRA2660
         SL    R4,C1M          SUBTRACT 68                               LLRA2670
         IC    R4,0(R4,R13)    OBTAIN CONSTANT FROM TABLE                LLRA2680
         STC   R4,NWRD+1       STORE IN SECOND BYTE OF NWRD              LLRA2690
         SRL   R5,8            SHIFT REMAINING 24 BITS RIGHT THEN OR ON  LLRA2700
         ALR   R5,R10          EXPONENT TO MAKE .(24 BITS)/16            LLRA2710
         ST    R5,0(R7,R6)     STORE IN CALLER'S ARRAY                   LLRA2720
         LE    FR0,NWRD        LOAD CHARACTERISTIC TO FLOATING POINT     LLRA2730
         SE    FR0,0(R7,R6)    REGISTER 0 AND SUBTRACT FRACTION          LLRA2740
         STE   FR0,0(R7,R6)    STORE NORMAL DEVIATE IN CALLER'S ARRAY    LLRA2750
         LR    R5,R0           COPY BACK TO R5 FOR NEXT GC AROUND        LLRA2760
         BR    R12             GO TO BXLE AND CONTINUE                   LLRA2770
F3       CL    R5,C3           R5 LESS THAN X'E2F00000' ?                LLRA2780
         BC    11,F4           NO                                        LLRA2790
         SLDL  R4,12           SHIFT FIRST 12 BITS OF R5 INTO R4         LLRA2800
         SL    R4,C2M          SUBTRACT CE8                              LLRA2810
         IC    R4,0(R4,R13)    OBTAIN CONSTANT FROM TABLE                LLRA2820
         STC   R4,PWRD+1       STORE IN SECOND BYTE OF PWRD              LLRA2830
         SRL   R5,8            SHIFT REMAINING 20 BITS RIGHT THEN OR ON  LLRA2840
         ALR   R5,R10          EXPONENT TO MAKE .(20 BITS)/16            LLRA2850
         ST    R5,0(R7,R6)     STORE IN CALLER'S ARRAY                   LLRA2860
         LE    FR0,PWRD        LOAD CHARACTERISTIC TO FLOATING POINT     LLRA2870
         AE    FR0,0(R7,R6)    REGISTER 0 AND ADD FRACTION               LLRA2880
         STE   FR0,0(R7,R6)    STORE NORMAL DEVIATE IN CALLER'S ARRAY    LLRA2890
         LR    R5,R0           COPY BACK TO R5 FOR NEXT GC AROUND        LLRA2900
         BR    R12             GO TO BXLE AND CONTINUE                   LLRA2910
F4       CL    R5,C4           R5 LESS THAN X'F5E00000' ?                LLRA2920
         BC    11,F5           NO                                        LLRA2930
         SLDL  R4,12           SHIFT FIRST 12 BITS OF R5 INTO R4         LLRA2940
         SL    R4,C3M          SUBTRACT E17                              LLRA2950
         IC    R4,0(R4,R13)    OBTAIN CONSTANT FROM TABLE                LLRA2960
         STC   R4,NWRD+1       STORE AS SECOND BYTE OF NWRD              LLRA2970
         SRL   R5,8            SHIFT REMAINING 20 BITS RIGHT THEN OR ON  LLRA2980
         ALR   R5,R10          EXPONENT TO MAKE .(20 BITS)/16            LLRA2990
         ST    R5,0(R7,R6)     STORE IN CALLER'S ARRAY                   LLRA3000
         LE    FR0,NWRD        LOAD CHARACTERISTIC TO FLOATING POINT     LLRA3010
         SE    FR0,0(R7,R6)    REGISTER 0 AND SUBTRACT FRACTION          LLRA3020
         STE   FR0,0(R7,R6)    STORE NORMAL DEVIATE IN CALLER'S ARRAY    LLRA3030
         LR    R5,R0           COPY BACK TO R5 FOR NEXT GC AROUND        LLRA3040
         BR    R12             GO TO BXLE AND CONTINUE                   LLRA3050
F5       ST    R5,FWRD         STORE R5 IN ARGUMENT LIST                 LLRA3060
         ST    R0,XWRD         PASS STARTING VALUE                       LLRA3070
         LA    R13,SA2         LOAD LOW SAVE AREA POINTER                LLRA3080
         LA    R1,FLIST        ARGUMENT LIST FOR CALL TC RNORTH          LLRA3090
         LR    R8,R15          COPY BASE REGISTER FOR BALR LINKAGE       LLRA3100
         L     R15,ARNOR       ADDRESS OF FUNCTION SUBRCUTINE RNORTH     LLRA3110
         BALR  R14,R15         BRANCH TO RNORTH                          LLRA3120
         LR    R15,R8          RESTORE BASE REGISTER                     LLRA3130
         STE   FR0,0(R7,R6)    STORE NORMAL DEVIATE IN CALLER'S ARRAY    LLRA3140
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***** NAVAL POSTGRADUATE SCHOOL RANDOM NUMBER GENERATOR : LLRANDOM *****

         L      R5,XWRD           NEW STARTING VALUE                          LLRA3150
         LA     R13,ATBLE         RESTORE R13 TO TABLE OF CONSTANTS           LLRA3160
N5       BXLE   R7,R2,L5          LOOP AROUND AGAIN                           LLRA3170
         L      R13,SA2+4         RESTORE HIGH SAVE AREA POINTER              LLRA3180
         L      R1,24(,13)        GET ARGUMENT LIST POINTER AGAIN             LLRA3190
         L      R4,0(,R1)         GET STARTING VALUE ADDRESS AGAIN            LLRA3200
         ST     R5,0(,R4)         STORE AS STARTING VALUE FOR NEXT CALL       LLRA3210
         LM     R14,R12,12(R13)   RESTORE THE REGISTERS                       LLRA3220
         BCR    15,R14            RETURN                                      LLRA3230
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*                                                                       LLRA3250
*     ENTRY POINT : SNORM                                               LLRA3260
*                                                                       LLRA3270
          CNOP  0,8                                                     LLRA3280
          USING SNORM,R15       BASE REGISTER                           LLRA3290
SNORM     B     10(,R15)        BRANCH AROUND ID                        LLRA3300
          DC    AL1(5)                                                  LLRA3310
          DC    CL5'SNORM'                                              LLRA3320
          STM   R14,R12,12(R13) SAVE REGISTERS IN HIGH SAVE AREA        LLRA3330
          ST    R13,SA2+4       ADDRESS OF HIGH SAVE AREA IN LOW SAVE AR. LLRA3340
          LR    R2,R13          COPY TO R2                              LLRA3350
          LA    R13,SA2         ADDRESS OF LOW SAVE AREA                LLRA3360
          ST    R13,8(,R2)      ADDRESS OF LOW SAVE AREA IN HIGH SAVE AR. LLRA3370
          LM    R9,R11,A75N     LOAD MULTIPLIER,EXPONENT,AND TEST MASK  LLRA3380
          LA    R2,4            CONSTANT FOR BXLE                       LLRA3390
          LM    R5,R7,0(R1)     ADDRESSES OF THREE ARGUMENTS            LLRA3400
          L     R5,0(,R5)       LOAD STARTING VALUE INTO R5             LLRA3410
          L     R3,0(,R7)       NUMBER OF CONSECUTIVE WORDS TO FILL     LLRA3420
          SLA   R3,2            CONVERT TO BYTES                        LLRA3430
          SR    R6,R2           BACKUP ONE WORD IN CALLER'S ARRAY       LLRA3440
          LR    R7,R2           INITIAL VALUE FOR INDEX REGISTER        LLRA3450
          LA    R13,ATBLE       ADDRESS OF TABLE OF CONSTANTS           LLRA3460
          LA    R8,TABLE        ADDRESS OF SHUFFLING TABLE              LLRA3470
          LA    R12,N6          ADDRESS OF BXLE                         LLRA3480
          L     R1,MASK         INDEX MASK FOR SHUFFLING                LLRA3490
          CNOP  0,8             ALIGN BXLE LOOP FOR SPEED               LLRA3500
L6        MR    R4,R9           FORM PRODUCT OF A AND X(N-1)            LLRA3510
          SLDA  R4,1            R4 = REMAINDER ; R5= QUOTIENT           LLRA3520
          SRL   R5,1              ADD QUOTIENT TO REMAINDER THEREBY     LLRA3530
          AR    R4,R5               SIMULATING DIVISION BY 2**31-1      LLRA3540
          LR    R5,R4           PUT X(N) INTO R5                        LLRA3550
          NR    R4,R1           EXTRACT RIGHT-MOST 7 BITS               LLRA3560
          SLA   R4,2            CONVERT TO BYTE OFFSET IN TABLE         LLRA3570
          L     R0,0(R4,R8)     SELECT RANDOM TABLE VALUE               LLRA3580
          ST    R5,0(R4,R8)     REPLACE TABLE VALUE WITH X(N)           LLRA3590
          XR    R0,R5           EXCHANGE R0 AND R5                      LLRA3600
          XR    R5,R0             BY EXCLUSIVE OR'ING                   LLRA3610
          XR    R0,R5               THEM WITH EACH OTHER                LLRA3620
          NR    R4,R11          SHOULD WE MAKE IT NEGATIVE ?            LLRA3630
          BC    8,F1S           POSITIVE, KEEP GOING                    LLRA3640
          LNR   R5,R5           MAKE R5 TRUE NEGATIVE                   LLRA3650
          SLR   R4,R4           CLEAR R4 TO ZERO                        LLRA3660
F1S       CL    R5,C1           R5 LESS THAN X'68000000' ?              LLRA3670
          BC    11,F2S          NO                                      LLRA3680
          SLDL  R4,8            SHIFT FIRST 8 BITS OF R5 INTO R4 AS INDEX LLRA3690
          IC    R4,0(R4,R13)    OBTAIN CONSTANT FROM TABLE              LLRA3700
          STC   R4,PWRD+1       STORE IN SECOND BYTE OF PWRD            LLRA3710
          SRL   R5,8            SHIFT REMAINING 24 BITS RIGHT THEN OR ON LLRA3720
          ALR   R5,R10          EXPONENT TO MAKE  .(24 BITS)/16         LLRA3730
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         ST     R5,0(R7,R6)     STORE IN CALLER'S ARRAY                        LLRA3740
         LE     FR0,PWRD        LOAD CHARACTERISTIC TO FLOATING POINT          LLRA3750
         AE     FR0,0(R7,R6)    REGISTER 0 AND ADD FRACTION                    LLRA3760
         STE    FR0,0(R7,R6)    STORE NORMAL DEVIATE IN CALLER'S ARRAY         LLRA3770
         LR     R5,R0           COPY BACK TO R5 FOR NEXT GO AROUND             LLRA3780
         BR     R12             GO TO BXLE AND CONTINUE                        LLRA3790
F2S      CL     R5,C2           R5 LESS THAN X'D0000000' ?                     LLRA3800
         BC     11,F3S          NO                                             LLRA3810
         SLDL   R4,8            SHIFT FIRST 8 BITS OF R5 INTO R4 AS INDEX      LLRA3820
         SL     R4,C1M          SUBTRACT 68                                    LLRA3830
         IC     R4,0(R4,R13)    OBTAIN CONSTANT FROM TABLE                     LLRA3840
         STC    R4,NWRD+1       STORE IN SECOND BYTE OF NWRD                   LLRA3850
         SRL    R5,8            SHIFT REMAINING 24 BITS RIGHT THEN OR ON       LLRA3860
         ALR    R5,R10          EXPONENT TO MAKE .(24 BITS)/16                 LLRA3870
         ST     R5,0(R7,R6)     STORE IN CALLER'S ARRAY                        LLRA3880
         LE     FR0,NWRD        LOAD CHARACTERISTIC TO FLOATING POINT          LLRA3890
         SE     FR0,0(R7,R6)    REGISTER 0 AND SUBTRACT FRACTION               LLRA3900
         STE    FR0,0(R7,R6)    STORE NORMAL DEVIATE IN CALLER'S ARRAY         LLRA3910
         LR     R5,R0           COPY BACK TO R5 FOR NEXT GO AROUND             LLRA3920
         BR     R12             GO TO BXLE AND CONTINUE                        LLRA3930
F3S      CL     R5,C3           R5 LESS THAN X'E2F00000' ?                     LLRA3940
         BC     11,F4S          NO                                             LLRA3950
         SLDL   R4,12           SHIFT FIRST 12 BITS OF R5 INTO R4              LLRA3960
         SL     R4,C2M          SUBTRACT CE8                                   LLRA3970
         IC     R4,0(R4,R13)    OBTAIN CONSTANT FROM TABLE                     LLRA3980
         STC    R4,PWRD+1       STORE IN SECOND BYTE OF PWRD                   LLRA3990
         SRL    R5,8            SHIFT REMAINING 20 BITS RIGHT THEN OR ON       LLRA4000
         ALR    R5,R10          EXPONENT TO MAKE .(20 BITS)/16                 LLRA4010
         ST     R5,0(R7,R6)     STORE IN CALLER'S ARRAY                        LLRA4020
         LE     FR0,PWRD        LOAD CHARACTERISTIC TO FLOATING POINT          LLRA4030
         AE     FR0,0(R7,R6)    REGISTER 0 AND ADD FRACTION                    LLRA4040
         STE    FR0,0(R7,R6)    STORE NORMAL DEVIATE IN CALLER'S ARRAY         LLRA4050
         LR     R5,R0           COPY BACK TO R5 FOR NEXT GO AROUND             LLRA4060
         BR     R12             GO TO BXLE AND CONTINUE                        LLRA4070
F4S      CL     R5,C4           R5 LESS THAN X'F5E00000' ?                     LLRA4080
         BC     11,F5S          NO                                             LLRA4090
         SLDL   R4,12           SHIFT FIRST 12 BITS OF R5 INTO R4              LLRA4100
         SL     R4,C3M          SUBTRACT E17                                   LLRA4110
         IC     R4,0(R4,R13)    OBTAIN CONSTANT FROM TABLE                     LLRA4120
         STC    R4,NWRD+1       STORE AS SECOND BYTE OF NWRD                   LLRA4130
         SRL    R5,8            SHIFT REMAINING 20 BITS RIGHT THEN OR ON       LLRA4140
         ALR    R5,R10          EXPONENT TO MAKE .(20 BITS)/16                 LLRA4150
         ST     R5,0(R7,R6)     STORE IN CALLER'S ARRAY                        LLRA4160
         LE     FR0,NWRD        LOAD CHARACTERISTIC TO FLOATING POINT          LLRA4170
         SE     FR0,0(R7,R6)    REGISTER 0 AND SUBTRACT FRACTION               LLRA4180
         STE    FR0,0(R7,R6)    STORE NORMAL DEVIATE IN CALLER'S ARRAY         LLRA4190
         LR     R5,R0           COPY BACK TO R5 FOR NEXT GO AROUND             LLRA4200
         BR     R12             GO TO BXLE AND CONTINUE                        LLRA4210
F5S      ST     R5,FWRD         STORE R5 IN ARGUMENT LIST                      LLRA4220
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         ST     R0,XWRD          PASS STARTING VALUE                          LLRA4230
         LA     R13,SA2          LOAD LOW SAVE AREA POINTER                   LLRA4240
         LA     R1,FLIST         ARGUMENT LIST FOR CALL TC RNORTH             LLRA4250
         LR     R8,R15           COPY BASE FOR BALR LINKAGE                   LLRA4260
         L      R15,ARNOR        ADDRESS OF FUNCTION SUBROUTINE RNORTH        LLRA4270
         BALR   R14,R15          BRANCH TO RNORTH                             LLRA4280
         LR     R15,R8           RESTORE BASE REGISTER                        LLRA4290
         STE    FR0,0(R7,R6)     STORE NORMAL DEVIATE IN CALLER'S ARRAY       LLRA4300
         L      R5,XWRD          NEW STARTING VALUE                           LLRA4310
         LA     R13,ATBLE        RESTORE R13 TO TABLE OF CONSTANTS            LLRA4320
         LA     R8,TABLE         RESTORE R8 TO ADDRESS OF SHUFFLING TABLE     LLRA4330
         L      R1,MASK          RESTORE R1 TO INDEX MASK                     LLRA4340
N6       BXLE   R7,R2,L6         LOOP AROUND AGAIN                            LLRA4350
         L      R13,SA2+4        RESTORE HIGH SAVE AREA POINTER               LLRA4360
         L      R1,24(,R13)      GET ARGUMENT LIST POINTER AGAIN              LLRA4370
         L      R4,0(,R1)        GET STARTING VALUE ADDRESS AGAIN             LLRA4380
         ST     R5,0(,R4)        STORE AS STARTING VALUE FOR NEXT CALL        LLRA4390
         LM     R14,R12,12(R13)  RESTORE THE REGISTERS                        LLRA4400
         BCR    15,R14           RETURN                                       LLRA4410
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*                                                                      LLRA4430
*     ENTRY POINT :  EXPON                                             LLRA4440
*                                                                      LLRA4450
          CNOP  0,8                                                    LLRA4460
          USING EXPON,R15       BASE REGISTER                          LLRA4470
EXPON     B     10(,R15)        BRANCH AROUND ID                       LLRA4480
          DC    AL1(5)                                                 LLRA4490
          DC    CL5'EXPON'                                             LLRA4500
          STM   R14,R12,12(R13) SAVE REGISTERS IN HIGH SAVE AREA       LLRA4510
          ST    R13,SA2+4       ADDRESS OF HIGH SAVE AREA IN LOW SAVE AR. LLRA4520
          LR    R2,R13          COPY TO R2                             LLRA4530
          LA    R13,SA2         ADDRESS OF LOW SAVE AREA               LLRA4540
          ST    R13,8(,R2)      ADDRESS OF LOW SAVE AREA IN HIGH SAVE AR. LLRA4550
          LM    R9,R11,A75N     LOAD MULTIPLIER,EXPONENT,AND TEST MASK LLRA4560
          LA    R2,4            CONSTANT FOR BXLE                      LLRA4570
          LM    R5,R7,0(R1)     ADDRESSES OF THREE ARGUMENTS           LLRA4580
          L     R5,0(,R5)       LOAD STARTING VALUE INTO R5            LLRA4590
          L     R3,0(,R7)       NUMBER OF CONSECUTIVE WORDS TO FILL    LLRA4600
          SLA   R3,2            CONVERT TO BYTES                       LLRA4610
          SR    R6,R2           BACKUP ONE WORD IN CALLER'S ARRAY      LLRA4620
          LR    R7,R2           INITIAL VALUE FOR INDEX REGISTER       LLRA4630
          LA    R13,BTBLE       ADDRESS OF TABLE OF CONSTANTS          LLRA4640
          LA    R12,N7          ADDRESS OF BXLE                        LLRA4650
          CNOP  0,8             ALIGN BXLE LOOP FOR SPEED              LLRA4660
L7        MR    R4,R9           FORM PRODUCT OF A AND X(N-1)           LLRA4670
          SLDA  R4,1            R4 = REMAINDER ; R5 = QUOTIENT         LLRA4680
          SRL   R5,1              ADD QUOTIENT TO REMAINDER THEREBY    LLRA4690
          AR    R4,R5               SIMULATING DIVISION BY 2**31-1     LLRA4700
          LR    R5,R4           PUT X(N) INTO R5                       LLRA4710
          LR    R0,R5           COPY R5 INTO R0 FOR NOW                LLRA4720
          NR    R4,R11          SHOULD WE MAKE IT NEGATIVE ?           LLRA4730
          BC    8,E1            POSITIVE, KEEP GOING                   LLRA4740
          LNR   R5,R5           MAKE R5 TRUE NEGATIVE                  LLRA4750
          SLR   R4,R4           CLEAR R4 TO ZERO                       LLRA4760
E1        CL    R5,D1           R5 LESS THAN X'D5000000' ?             LLRA4770
          BC    11,E2           NO                                     LLRA4780
          SLDL  R4,8            SHIFT FIRST 8 BITS OF R5 INTO R4 AS INDEX LLRA4790
          IC    R4,0(R4,R13)    OBTAIN CONSTANT FROM TABLE             LLRA4800
          STC   R4,PWRD+1       STORE IN SECOND BYTE OF PWRD           LLRA4810
          SRL   R5,8            SHIFT REMAINING 24 BITS RIGHT THEN OR ON LLRA4820
          ALR   R5,R10          EXPONENT TO MAKE .(24 BITS)/16         LLRA4830
          ST    R5,0(R7,R6)     STORE IN CALLER'S ARRAY                LLRA4840
          LE    FR0,PWRD        LOAD CHARACTERISTIC TO FLOATING POINT  LLRA4850
          AE    FR0,0(R7,R6)    REGISTER 0 AND ADD FRACTION            LLRA4860
          STE   FR0,0(R7,R6)    STORE EXPONENTIAL DEVIATE IN ARRAY     LLRA4870
          LR    R5,R0           COPY BACK TO R5 FOR NEXT GO AROUND     LLRA4880
          BR    R12             GO TO BXLE AND CONTINUE                LLRA4890
E2        CL    R5,D2           R5 LESS THAN X'F1700000' ?             LLRA4900
          BC    11,E3           NO                                     LLRA4910
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***** NAVAL POSTGRADUATE SCHOOL RANDOM NUMBER GENERATOR : LLRANDOM *****

         SLDL  R4,12            SHIFT FIRST 12 BITS OF R5 INTO R4          LLRA4920
         SL    R4,DIM           SUBTRACT OFF                               LLRA4930
         IC    R4,0(R4,R13)     OBTAIN CONSTANT FROM TABLE                 LLRA4940
         STC   R4,PWRD+1        STORE AS SECOND BYTE OF PWRD               LLRA4950
         SRL   R5,8             SHIFT REMAINING 20 BITS RIGHT THEN OR ON   LLRA4960
         ALR   R5,R10           EXPONENT TO MAKE .(20 BITS)/16             LLRA4970
         ST    R5,0(R7,R6)      STORE IN CALLER'S ARRAY                    LLRA4980
         LE    FR0,PWRD         LOAD CHARACTERISTIC TO FLOATING POINT      LLRA4990
         AE    FR0,0(R7,R6)     REGISTER 0 AND ADD FRACTION                LLRA5000
         STE   FR0,0(R7,R6)     STORE EXPONENTIAL DEVIATE IN ARRAY         LLRA5010
         LR    R5,R0            COPY BACK TO R5 FOR NEXT GO AROUND         LLRA5020
         BR    R12              GO TO BXLE AND CONTINUE                    LLRA5030
E3       ST    R5,EWRD          STORE R5 IN ARGUMENT LIST                  LLRA5040
         ST    R0,XWRD          PASS STARTING VALUE                        LLRA5050
         LA    R13,SA2          LOAD LOW SAVE AREA POINTER                 LLRA5060
         LA    R1,ELIST         ARGUMENT LIST FOR CALL TO REXPTH           LLRA5070
         LR    R8,R15           COPY BASE REGISTER FOR BALR LINKAGE        LLRA5080
         L     R15,AREXP        ADDRESS OF FUNCTION SUBROUTINE REXPTH      LLRA5090
         BALR  R14,R15          BRANCH TO REXPTH                           LLRA5100
         LR    R15,R8           RESTORE BASE REGISTER                      LLRA5110
         STE   FR0,0(R7,R6)     STORE EXPONENTIAL DEVIATE IN ARRAY         LLRA5120
         L     R5,XWRD          NEW STARTING VALUE                         LLRA5130
         LA    R13,BTBLE        RESTORE R13 TO TABLE OF CONTENTS           LLRA5140
N7       BXLE  R7,R2,L7         LOOP AROUND AGAIN                          LLRA5150
         L     R13,SA2+4        RESTORE HIGH SAVE AREA POINTER             LLRA5160
         L     R1,24(,R13)      GET ARGUMENT LIST POINTER AGAIN            LLRA5170
         L     R4,0(,R1)        GET STARTING VALUE ADDRESS AGAIN           LLRA5180
         ST    R5,0(,R4)        STORE AS STARTING VALUE FOR NEXT CALL      LLRA5190
         LM    R14,R12,12(R13)  RESTORE THE REGISTERS                      LLRA5200
         BCR   15,R14           RETURN                                     LLRA5210
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*                                                                      LLRA5230
*     ENTRY POINT :  SEXPON                                            LLRA5240
*                                                                      LLRA5250
          CNOP  0,8                                                    LLRA5260
          USING SEXPON,R15      BASE REGISTER                          LLRA5270
SEXPON    B     12(,R15)        BRANCH AROUND ID                       LLRA5280
          DC    AL1(6)                                                 LLRA5290
          DC    CL6'SEXPON'                                            LLRA5300
          STM   R14,R12,12(R13) SAVE REGISTERS IN HIGH SAVE AREA       LLRA5310
          ST    R13,SA2+4       ADDRESS OF HIGH SAVE AREA IN LOW SAVE AR. LLRA5320
          LR    R2,R13          COPY TO R2                             LLRA5330
          LA    R13,SA2         ADDRESS OF LOW SAVE AREA               LLRA5340
          ST    R13,8(,R2)      ADDRESS OF LOW SAVE AREA IN HIGH SAVE AR. LLRA5350
          LM    R9,R11,A75N     LOAD MULTIPLIER,EXPONENT,AND TEST MASK LLRA5360
          LA    R2,4            CONSTANT FOR BXLE                      LLRA5370
          LM    R5,R7,0(R1)     ADDRESSES OF THREE ARGUMENTS           LLRA5380
          L     R5,0(,R5)       LOAD STARTING VALUE IN R5              LLRA5390
          L     R3,0(,R7)       NUMBER OF CONSECUTIVE WORDS TO FILL    LLRA5400
          SLA   R3,2            CONVERT TO BYTES                       LLRA5410
          SR    R6,R2           BACKUP ONE WORD IN CALLER'S ARRAY      LLRA5420
          LR    R7,R2           INITIAL VALUE FOR INDEX REGISTER       LLRA5430
          LA    R13,BTBLE       ADDRESS OF TABLE OF CONSTANTS          LLRA5440
          LA    R8,TABLE        ADDRESS OF SHUFFLING TABLE             LLRA5450
          LA    R12,N8          ADDRESS OF BXLE                        LLRA5460
          L     R1,MASK         INDEX MASK FOR SHUFFLING               LLRA5470
          CNOP  0,8             ALIGN BXLE LOOP FOR SPEED              LLRA5480
L8        MR    R4,R9           FORM PRODUCT OF A AND X(N-1)           LLRA5490
          SLDA  R4,1            R4 = QUOTIENT ; R5 = REMAINDER         LLRA5500
          SRL   R5,1              ADD QUOTIENT TO REMAINDER THEREBY    LLRA5510
          AR    R4,R5               SIMULATING DIVISION BY 2**31-1     LLRA5520
          LR    R5,R4           PUT X(N) INTO R5                       LLRA5530
          NR    R4,R1           EXTRACT RIGHT-MOST 7 BITS              LLRA5540
          SLA   R4,2            CONVERT TO BYTE OFFSET IN TABLE        LLRA5550
          L     R0,0(R4,R8)     SELECT RANDOM TABLE VALUE              LLRA5560
          ST    R5,0(R4,R8)     REPLACE TABLE VALUE WITH X(N)          LLRA5570
          XR    R0,R5           EXCHANGE R0 AND R5                     LLRA5580
          XR    R5,R0             BY EXCLUSIVE OR'ING                  LLRA5590
          XR    R0,R5               THEM WITH EACH OTHER               LLRA5600
          NR    R4,R11          SHOULD WE MAKE IT NEGATIVE ?           LLRA5610
          BC    8,E1S           POSITIVE, KEEP GOING                   LLRA5620
          LNR   R5,R5           MAKE R5 TRUE NEGATIVE                  LLRA5630
          SLR   R4,R4           CLEAR R4 TO ZERO                       LLRA5640
E1S       CL    R5,D1           R5 LESS THAN X'D5000000' ?             LLRA5650
          BC    11,E2S          NO                                     LLRA5660
          SLDL  R4,8            SHIFT FIRST 8 BITS OF R5 INTO R4 AS INDEX LLRA5670
          IC    R4,0(R4,R13)    OBTAIN CONSTANT FROM TABLE             LLRA5680
          STC   R4,PWRD+1       STORE IN SECOND BYTE OF PWRD           LLRA5690
          SRL   R5,8            SHIFT REMAINING 24 BITS RIGHT THEN OR ON LLRA5700
          ALR   R5,R10          EXPONENT TO MAKE .(24 BITS)/16         LLRA5710
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         ST     R5,0(R7,R6)      STORE IN CALLER'S ARRAY                        LLRA5720
         LE     FR0,PWRD         LOAD CHARACTERISTIC TO FLOATING POINT          LLRA5730
         AE     FR0,0(R7,R6)     REGISTER 0 AND ADD FRACTION                    LLRA5740
         STE    FR0,0(R7,R6)     STORE EXPONENTIAL DEVIATE IN ARRAY             LLRA5750
         LR     R5,R0            COPY BACK TO R5 FOR NEXT GC AROUND             LLRA5760
         BR     R12              GO TO BXLE AND CONTINUE                        LLRA5770
E2S      CL     R5,D2            R5 LESS THAN X'F1700000' ?                     LLRA5780
         BC     11,E3S           NO                                             LLRA5790
         SLDL   R4,12            SHIFT FIRST 12 BITS OF R5 INTO R4              LLRA5800
         SL     R4,DIM           SUBTRACT OFF                                   LLRA5810
         IC     R4,0(R4,R13)     OBTAIN CONSTANT FROM TABLE                     LLRA5820
         STC    R4,PWRD+1        STORE AS SECOND BYTE OF PWRD                   LLRA5830
         SRL    R5,8             SHIFT REMAINING 20 BITS RIGHT THEN OR ON       LLRA5840
         ALR    R5,R10           EXPONENT TO MAKE .(20 BITS)/16                 LLRA5850
         ST     R5,0(R7,R6)      STORE IN CALLER'S ARRAY                        LLRA5860
         LE     FR0,PWRD         LOAD CHARACTERISTIC TO FLOATING POINT          LLRA5870
         AE     FR0,0(R7,R6)     REGISTER 0 AND ADD FRACTION                    LLRA5880
         STE    FR0,0(R7,R6)     STORE EXPONENTIAL DEVIATE IN ARRAY             LLRA5890
         LR     R5,R0            COPY BACK TO R5 FOR NEXT GC AROUND             LLRA5900
         BR     R12              GO TO BXLE AND CONTINUE                        LLRA5910
E3S      ST     R5,EWRD          STORE R5 IN ARGUMENT LIST                      LLRA5920
         ST     R0,XWRD          PASS STARTING VALUE                            LLRA5930
         LA     R13,SA2          LOAD LOW SAVE AREA POINTER                     LLRA5940
         LA     R1,ELIST         ARGUMENT LIST FOR CALL TO REXPTH               LLRA5950
         LR     R8,R15           COPY BASE FOR BALR LINKAGE                     LLRA5960
         L      R15,AREXP        ADDRESS OF FUNCTION SUBROUTINE REXPTH          LLRA5970
         BALR   R14,R15          BRANCH TO REXPTH                               LLRA5980
         LR     R15,R8           RESTORE BASE REGISTER                          LLRA5990
         STE    FR0,0(R7,R6)     STORE EXPONENTIAL DEVIATE IN ARRAY             LLRA6000
         L      R5,XWRD          NEW STARTING VALUE                             LLRA6010
         LA     R13,BTBLE        RESTORE R13 TO TABLE OF CONTENTS               LLRA6020
         LA     R8,TABLE         RESTORE R8 TO ADDRESS OF SHUFFLING TABLE       LLRA6030
         L      R1,MASK          RESTORE R1 TO INDEX MASK                       LLRA6040
N8       BXLE   R7,R2,L8         LOOP AROUND AGAIN                              LLRA6050
         L      R13,SA2+4        RESTORE HIGH SAVE AREA POINTER                 LLRA6060
         L      R1,24(,R13)      GET ARGUMENT LIST POINTER AGAIN                LLRA6070
         L      R4,0(,R1)        GET STARTING VALUE ADDRESS AGAIN               LLRA6080
         ST     R5,0(,R4)        STORE AS STARTING VALUE FOR NEXT CALL          LLRA6090
         LM     R14,R12,12(R13)  RESTORE THE REGISTERS                          LLRA6100
         BCR    15,R14           RETURN                                         LLRA6110
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*                                                                      LLRA6130
*     CONSTANTS AND STORAGE                                            LLRA6140
*                                                                      LLRA6150
SA        DS    18F                                                    LLRA6160
SA2       DS    18F                                                    LLRA6170
PICA      DS    F                                                      LLRA6180
PM2       DC    F'2147483645'                                          LLRA6190
A75       DC    F'16807'                                               LLRA6200
          DC    X'40000001'                                            LLRA6210
          DC    X'40100000'                                            LLRA6220
A75N      DC    F'16807'                                               LLRA6230
          DC    X'3F000000'                                            LLRA6240
          DC    X'00000040'                                            LLRA6250
MASK      DC    X'0000007F'                                            LLRA6260
PWRD      DC    X'41AA0000'                                            LLRA6270
NWRD      DC    X'C1AA0000'                                            LLRA6280
C1        DC    X'68000000'                                            LLRA6290
C2        DC    X'D0000000'                                            LLRA6300
C3        DC    X'E2F00000'                                            LLRA6310
C4        DC    X'F5E00000'                                            LLRA6320
C1M       DC    X'00000068'                                            LLRA6330
C2M       DC    X'00000CE8'                                            LLRA6340
C3M       DC    X'00000E17'                                            LLRA6350
D1        DC    X'D5000000'                                            LLRA6360
D2        DC    X'F1700000'                                            LLRA6370
D1M       DC    X'00000CFF'                                            LLRA6380
FWRD      DS    F                                                      LLRA6390
EWRD      DS    F                                                      LLRA6400
XWRD      DS    F                                                      LLRA6410
FLIST     DC    AL4(FWRD)                                              LLRA6420
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R3       EQU   3                                                        LLRA7420
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R6       EQU   6                                                        LLRA7450
R7       EQU   7                                                        LLRA7460
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R11      EQU   11                                                       LLRA7500
R12      EQU   12                                                       LLRA7510
R13      EQU   13                                                       LLRA7520
R14      EQU   14                                                       LLRA7530
R15      EQU   15                                                       LLRA7540
FR0      EQU   0                                                        LLRA7550
FR2      EQU   2                                                        LLRA7560
         END                                                            LLRA7570
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Naval Postgraduate School
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3. ABSTRACT

This report is intended to describe an interim version of a computer program package for random number generation on the IBM System/360. The package, when called by a FORTRAN IV program, will deliver either a single value or an array (of specified size) of single precision uniformly, normally, or exponentially distributed pseudo-random deviates, or a single value or an array of uniformly distributed integers between 1 and $2^{31}-1$. The package also has the ability (optional) to "shuffle" the pseudo-random numbers to obtain "better" statistical properties.

14 KEY WORDS	LINK A		LINK B		LINK C	
	ROLE	WT	ROLE	WT	ROLE	WT
Random number generator						
Pseudo-random numbers						
Normal distribution						
Exponential distribution						
Shuffled random numbers						
Division simulation						
Congruential generator						

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